

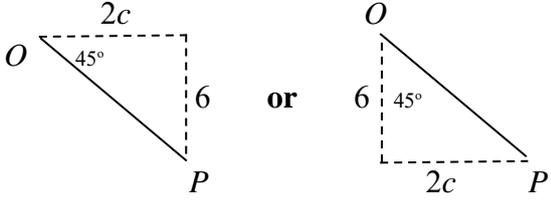
Question	Scheme		Marks	AOs
	Allow column vectors throughout this question			
<b>1(a)</b>	Differentiate $\mathbf{v}$ wrt $t$		M1	3.1a
	$\frac{3}{2}t^{-\frac{1}{2}}\mathbf{i} - 2\mathbf{j}$ isw		A1	1.1b
			(2)	
<b>1(b)</b>	$3t^{\frac{1}{2}} = 2t$		M1	2.1
	Solve for $t$		DM1	1.1b
	$t = \frac{9}{4}$		A1	1.1b
			(3)	
<b>1(c)</b>	Integrate $\mathbf{v}$ wrt $t$		M1	3.1a
	$\mathbf{r} = 2t^{\frac{3}{2}}\mathbf{i} - t^2\mathbf{j} (+\mathbf{C})$		A1	1.1b
	$t = 1, \mathbf{r} = -\mathbf{j} \Rightarrow \mathbf{C} = -2\mathbf{i}$ so $\mathbf{r} = 2t^{\frac{3}{2}}\mathbf{i} - t^2\mathbf{j} - 2\mathbf{i}$		A1	2.2a
			(3)	
<b>1(d)</b>	$\sqrt{(3t^{\frac{1}{2}})^2 + (2t)^2} = 10$ or $(3t^{\frac{1}{2}})^2 + (2t)^2 = 10^2$		M1	2.1
	$9t + 4t^2 = 100$		M(A)1	1.1b
	$t = 4$		A1	1.1b
	$\mathbf{r} = 14\mathbf{i} - 16\mathbf{j}$		M1	1.1b
	$\sqrt{14^2 + (-16)^2}$		M1	3.1a
	$\sqrt{452} (2\sqrt{113})$ (m)		A1	1.1b
			(6)	
<b>(14 marks)</b>				
Notes:				
<b>1a</b>	M1	Both powers decreasing by 1 (M0 if vector(s) disappear but allow recovery)		
	A1	cao		
<b>1b</b>	M1	Complete method, using $\mathbf{v}$ , to obtain an equation in $t$ only, allow a sign error		
	DM1	Dependent on M1, solve for $t$		

	A1	cao
<b>1c</b>	M1	Both powers increasing by 1 (M0 if vectors disappear but allow recovery)
	A1	Correct expression without <b>C</b>
	A1	cao
<b>1d</b>	M1	Use of Pythagoras on <b>v</b> and 10 to set up equation in $t$
	M(A)1	Correct 3 term quadratic in $t$
	A1	cao
	M1	Substitute their numerical $t$ value into their <b>r</b>
	M1	Use of Pythagoras to find the magnitude of their <b>r</b>
	A1	cso

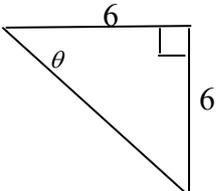
Question	Scheme		Marks	AOs
<b>2(a)</b>	Put $t = 2$ in $\mathbf{v}$ and use Pythagoras: $\sqrt{12^2 + (-6\sqrt{2})^2}$		M1	3.1a
	$\sqrt{216}, 6\sqrt{6}$ or 15 or better (m s <sup>-1</sup> )		A1	1.1b
			(2)	
<b>2(b)</b>	Differentiate $\mathbf{v}$ wrt $t$ to obtain $\mathbf{a}$		M1	3.4
	$6t\mathbf{i} - 3t^{-\frac{1}{2}}\mathbf{j}$ oe (m s <sup>-2</sup> ) isw		A1	1.1b
			(2)	
<b>2(c)</b>	Integrate $\mathbf{v}$ wrt $t$ to obtain $\mathbf{r}$		M1	3.4
	$\mathbf{r} = t^3\mathbf{i} - 4t^{\frac{3}{2}}\mathbf{j} (+\mathbf{C})$		A1	1.1b
	$(\mathbf{i} - 4\mathbf{j}) = 4^3\mathbf{i} - 4 \times 4^{\frac{3}{2}}\mathbf{j} + \mathbf{C}$		M1	3.1a
	$(-62\mathbf{i} + 24\mathbf{j})$ (m) isw e.g. if they go on to find the distance.		A1	1.1b
			(4)	
<b>(8 marks)</b>				
Notes: Accept column vectors throughout apart from the answer to (b).				
<b>2a</b>	M1	Need square root but -ve sign not required. Allow $\mathbf{i}$ 's and/or $\mathbf{j}$ 's to go missing from their $\mathbf{v}$ at $t = 2$ , provided they have applied Pythagoras correctly.		
	A1	cao <b>N.B.</b> Correct answer with no working can score 2 marks.		
<b>2b</b>	M1	Both powers decreasing by 1. Allow a column vector. M0 if $\mathbf{i}$ or $\mathbf{j}$ is missing but allow recovery in (b).		
	A1	cao. Do not accept a column vector.		
<b>2c</b>	M1	Both powers increasing by 1 M0 if $\mathbf{i}$ or $\mathbf{j}$ is missing but allow recovery.		
	A1	$(\mathbf{r} = )$ not required		
	M1	Putting $\mathbf{r} = (\mathbf{i} - 4\mathbf{j})$ and $t = 4$ into their displacement <b>vector</b> expression which must have $\mathbf{C}$ (allow $C$ ) to give an equation in $\mathbf{C}$ only, seen or implied. Must have attempted to integrate $\mathbf{v}$ for this mark to be available. <b>N.B.</b> $\mathbf{C}$ does not need to be found and <u>this is a method mark, so allow slips.</u>		
	A1	cao		

Question	Scheme		Marks	AOs
3(a)	7i – 3j seen or implied by Pythagoras		B1	1.1b
	Use Pythagoras: $\sqrt{7^2 + (-3)^2}$		M1	3.1a
	$\sqrt{58}$ , 7.6 or better ( m s <sup>-1</sup> )		A1	1.1b
			(3)	
3(b)	$t^2 - 3t + 7 = 2t^2 - 3$ OR $\frac{t^2 - 3t + 7}{2t^2 - 3} = \frac{1}{1} = 1$		M1	2.1
	t = 2 only		A1	1.1b
			(2)	
3(c)	Differentiate <b>v</b> wrt <i>t</i> to give a vector.		M1	3.1a
	$(2t - 3)\mathbf{i} + 4t\mathbf{j}$		A1	1.1b
			(2)	
3(d)	2t – 3 = 0		M1	3.1a
	t = 1.5		A1	1.1b
			(2)	
<b>(9 marks)</b>				
<b>Notes: Allow column vectors throughout.</b>				
3a	B1	cao		
	M1	Use of Pythagoras, including the square root, on a <b>velocity</b> vector at <i>t</i> = 0		
	A1	cao. Must come from a <u>correct</u> <b>v</b> .		
3b	M1	Equating <b>i</b> and <b>j</b> components of <b>v</b> or a ratio of 1:1 to obtain a quadratic in <i>t</i> only. If they use a constant, e.g. $t^2 - 3t + 7 = k$ and $2t^2 - 3 = k$ , <i>k</i> must be eliminated to earn this mark. <b>N.B.</b> M0 (since wrong working seen) if they write down $\mathbf{i} + \mathbf{j} = (t^2 - 3t + 7)\mathbf{i} + (2t^2 - 3)\mathbf{j}$  <b>OR</b> $\begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} t^2 - 3t + 7 \\ 2t^2 - 3 \end{pmatrix}$  <b>OR</b> $t^2 - 3t + 7 = 1$ and $2t^2 - 3 = 1$		

		and then $t^2 - 3t + 7 = 2t^2 - 3$
	A1	$t = 2$
		<b>N.B.</b> Allow M1A1 for a <b>correct</b> trial and error method where they obtain $\mathbf{v} = 5\mathbf{i} + 5\mathbf{j}$ when $t = 2$ but M0 if they don't get $t = 2$
<b>3c</b>	M1	At least one power decreasing by 1 in <b>each</b> component in their $\mathbf{v}$ (M0 if clearly dividing by $t$ ) <b>Both i and j</b> needed in their answer or a column vector Allow recovery if the <b>i</b> and <b>j</b> disappear and then reappear.
	A1	cao (must be a vector) isw e.g. if they find the magnitude or put $t = 0$ or differentiate again <b>i's</b> and <b>j's</b> do not need to be collected. <b>N.B.</b> Allow M1A0 for $2t - 3\mathbf{i} + 4t\mathbf{j}$
<b>3d</b>	M1	$2t - 3 = 0$ or (their <b>derivative</b> of the <b>i</b> -component of $\mathbf{v}$ ) = 0 <b>N.B.</b> M0 if they equate the derivative of both components of $\mathbf{v}$ to zero.
	A1	cao <b>N.B.</b> Correct answer, with no working, can score both marks.

Question	Scheme	Marks	AOs
4(a)	<b>ALTERNATIVES</b> when $t = 4$ is substituted at the beginning.		
	<p><math>2c\mathbf{i} - 6\mathbf{j}</math> or as a column vector, seen or implied.</p> <p><b>ALT 1</b></p>  <p><b>AND</b></p> <p><b>either</b> <math>\tan 45^\circ = \frac{2c}{6} \Rightarrow 2c = 6</math></p> <p><b>or</b> <b>states</b> isosceles triangle so <math>2c = 6</math></p> <p><b>N.B.</b> In both of the above, we must see the justification for the equation.</p> <p><b>ALT 2</b></p> $\tan 135^\circ = \frac{2c}{-6} \Rightarrow 2c = 6$ <p><b>N.B.</b> M0 if they are using the wrong bearing.</p>	B1	1.1b
	$c = 3$ *	A1*	2.2a
	<p><b>SC 1 M1A0:</b> no right-angled triangle <math>2c\mathbf{i} - 6\mathbf{j} = k(\mathbf{i} - \mathbf{j}) \Rightarrow 2c = 6</math> <b>or</b> <math>\mathbf{i}\cdot\text{cpt} = -\mathbf{j}\cdot\text{cpt} \Rightarrow 2c = 6</math></p> <p><b>N.B.</b> In both of the above, we must see the justification for the equation.</p> <p><b>SC 2 M1A0:</b> no right-angled triangle <math>\tan 45^\circ = \frac{2c}{6}</math> or <math>\frac{6}{2c} \Rightarrow 2c = 6</math></p> <p><b>N.B.</b> In the above, we must see the justification for the equation.</p>		

	<b>ALTERNATIVES</b> when $t = 4$ is substituted at the end:		
	$ct^{\frac{1}{2}} = 2c$ <b>and</b> $(-)\frac{3t^2}{8} = (-)6$ when $t = 4$ , seen or implied	B1	
	<p><b>ALT 3</b></p> <p><b>AND</b></p> <p><b>either</b> <math>\tan 45^\circ = \frac{\frac{3t^2}{8}}{ct^{\frac{1}{2}}} \Rightarrow 2c = 6</math> when <math>t = 4</math></p> <p><b>or</b> <b>states</b> isosceles triangle, so <math>ct^{\frac{1}{2}} = \frac{3t^2}{8} \Rightarrow 2c = 6</math> when <math>t = 4</math></p> <p><b>N.B.</b> In both of the above, we must see the justification for the equation.</p> <p><b>N.B.</b> M0 if they are using the wrong bearing.</p>	M1	
	$c = 3$	A1*	
	<p><b>SC 3 M1A0:</b> no right-angled triangle</p> $(ct^{\frac{1}{2}}\mathbf{i} - \frac{3t^2}{8}\mathbf{j}) = k(\mathbf{i} - \mathbf{j}) \Rightarrow 2c = 6$ when $t = 4$ <p><b>or</b> <math>\mathbf{i}\text{-cpt} = -\mathbf{j}\text{-cpt} \Rightarrow ct^{\frac{1}{2}} = \frac{3t^2}{8} \Rightarrow 2c = 6</math> when <math>t = 4</math></p> <p><b>N.B.</b> In both of the above, we must see the justification for the equation.</p> <p><b>SC 4 M1A0:</b> no right-angled triangle</p> $\tan 45^\circ = \frac{\frac{3t^2}{8}}{ct^{\frac{1}{2}}} \Rightarrow 2c = 6$ when $t = 4$ <p>.</p>		

	<p><b>N.B.</b> Allow a <b>verification</b>: i.e. use <math>c = 3</math> and <math>t = 4</math> to show that <math>P</math> is on a bearing of <math>135^\circ</math> from <math>O</math>.</p> <p><math>6\mathbf{i} - 6\mathbf{j}</math> then a diagram:</p>  <p><b>AND</b> <math>\tan \theta = \frac{6}{6}</math> or isosceles triangle <math>\Rightarrow \theta = 45^\circ</math></p> <p><b>N.B.</b> In the above, we must see the justification for the equation.</p>	B1	
		M1	
	bearing = $45^\circ + 90^\circ = 135^\circ$	A1*	
		(3)	
<b>4(b)</b>	Differentiate $\mathbf{r}$ wrt $t$ to obtain $\mathbf{v}$	M1	2.1
	$\mathbf{v} = 3 \times \frac{1}{2} t^{-\frac{1}{2}} \mathbf{i} - \frac{3}{8} \times 2t \mathbf{j} = \frac{3}{2} t^{-\frac{1}{2}} \mathbf{i} - \frac{3}{4} t \mathbf{j}$ oe	A1	1.1b
	Put $t = 4$ into <b>both</b> components and use Pythagoras: $\sqrt{\left(\frac{3}{4}\right)^2 + (-3)^2}$	M1	3.1a
	$\frac{\sqrt{153}}{\sqrt{16}}$ or $\frac{\sqrt{153}}{4}$ or $\frac{3\sqrt{17}}{4}$ or $3\sqrt{\frac{17}{16}} = 3.0923\dots$ (m s <sup>-1</sup> )	A1	1.1b
		(4)	
<b>4(c)</b>	Differentiate their $\mathbf{v}$ wrt $t$ to obtain $\mathbf{a}$	M1	3.4
	$\mathbf{a} = -\frac{3}{4} t^{-\frac{3}{2}} \mathbf{i} - \frac{3}{4} \mathbf{j}$	A1	1.1b
	$\frac{-\frac{3}{4} T^{-\frac{3}{2}}}{-\frac{3}{4}} = \frac{-1}{-27}$ oe	M1	2.1
	( $T =$ ) 9	A1	1.1b
		(4)	

(11 marks)		
Notes: Accept column vectors throughout		
<b>4a</b>	B1	$2c\mathbf{i} - 6\mathbf{j}$ seen or implied. B0 for $r = 2c - 6$ if no evidence of components.
	M1	<b>ALT 1:</b> Use the bearing to obtain a CORRECT diagram showing a right-angled triangle with at least one $45^\circ$ angle marked or clearly explained (i.e. $135^\circ$ marked on the diagram and either $135^\circ - 90^\circ = 45^\circ$ or $180^\circ - 135^\circ = 45^\circ$ ), and $2c$ and $\pm 6$ marked <b>AND</b> use of isosceles triangle or tan or (sin/cos and Pythag) to obtain $2c = 6$ <b>ALT 2: No diagram required</b> Use $\tan 135^\circ = \frac{2c}{-6} \Rightarrow 2c = 6$
	A1*	Given answer correctly obtained
		<b>ALTERNATIVE</b> when $t = 4$ is substituted at the end:
	B1	$ct^{\frac{1}{2}} = 2c$ <b>and</b> $(-)\frac{3t^2}{8} = (-)6$ when $t = 4$ , seen or implied
	M1	<b>ALT 3:</b> Use the bearing to obtain a CORRECT diagram showing a right-angled triangle with at least one $45^\circ$ angle marked or clearly explained (i.e. $135^\circ$ marked on the diagram and either $135^\circ - 90^\circ = 45^\circ$ or $180^\circ - 135^\circ = 45^\circ$ ), and $ct^{\frac{1}{2}}$ and $\pm \frac{3t^2}{8}$ marked <b>AND</b> use of isosceles triangle or tan or (sin/cos and Pythag) to obtain $2c = 6$ when $t = 4$
	A1*	Given answer correctly obtained
<b>4b</b>	M1	Both powers of $t$ decreasing by 1 (M0 if $\mathbf{i}$ or $\mathbf{j}$ is missing but allow recovery or working with components only) <b>N.B.</b> This mark is available if $c$ has not been substituted for.
	A1	Correct unsimplified derivative or two correct components
	M1	Put $t = 4$ in their $\mathbf{v}$ (must be using an attempted derivative of $\mathbf{r}$ ) and then use Pythagoras with the root, allow a missing $-$ sign <b>N.B.</b> If they <b>state</b> $t = 4$ , allow a slip when they substitute in, for this M mark. This mark is available if $c$ has not been substituted for.
	A1	Accept 3.1 or better
<b>4c</b>	M1	Both powers of $t$ decreasing by 1 <b>N.B.</b> This mark is available if $c$ has not been substituted for (M0 if $\mathbf{i}$ or $\mathbf{j}$ is missing but allow recovery or working with components only).
	A1	Correct unsimplified derivative
	M1	Use of an appropriate <b>ratio</b> (must be using an attempted derivative of <b>their v</b> ), condone sign error and the <b>reciprocal</b> , to obtain an equation in $t$ or <b>T only</b> . <b>N.B.</b> If they state that $-\frac{3}{4}T^{-\frac{3}{2}}\mathbf{i} - \frac{3}{4}\mathbf{j} = k(-\mathbf{i} - 27\mathbf{j})$ and then equate coefficients to give two simultaneous equations in $k$ and $T$ , these need to be used to produce an equation in <b>T only</b> , before the M mark is earned.
	A1	cao (allow $t$ instead of $T$ )